# Computer Lab in Economics: MATLAB Introduction to Optimization in MATLAB

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Computer Lab in Economics: MATLAB

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# Optimization in MATLAB

- MATLAB can solve two types of optimization problems:
  - Zero finding: Find x such f(x) = 0.
  - **Minimization**: min f(x)
- A maximization problem can be solved by minimizing the negative of the function: max f(x) = min - f(x).
- Zero finding of functions of one variable and minimization can be solved with basic MATLAB.
- For finding the zeros of functions of several variables and minimization with constraints a toolbox is needed. The official *Optimization Toolbox* provides this functionality.

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# Zero finding

- The function fzero is used to find the zero of a 1-D function.
- The objective function can be a function in a separate file or an anonymous function.
- For the solver to work, you must supply an initial guess of where the zero is or an interval in which the zero is located.
- If a function has several zeros, the result is conditioned by the initial guess.
- The function returns the value of x where the zero is located. The value y = f(x) is returned as the second argument.

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#### Zero Finding

### Zero Finding. Example



# Zero Finding. Example

```
% Define the objective function as an anonymous
function
objFun = @(x) sin(x) + cos(x);
```

```
% Plot the objective function
ezplot(objFun, [-3,3]);
```

```
% Optimize it with zero as initial guess
[x, val] = fzero(objFun, 0)
```

#### Zero Finding

# Zero Finding. Example

```
% Find the zero at the left
>> [x, val] = fzero(objFun, 0)
x =
-0.7854
val =
-1.1102e-16
% Find the zero at the right
>> [x, val] = fzero(objFun, [0 3])
x =
2.3562
val =
-5.5511e-16
```

## Minimization

- Minimization in one dimension is performed with the **fminbnd** functions.
- The function searches a minimum between a given interval (bound).
- Minimization of functions of several variables are performed with the **fminsearch** function.
- For the function, each variable is an element of a vector x.

#### Minimization. Example 1-D

```
% Define the objective function as an anonymous
function
objFun = @(x) sin(x) + cos(x);
```

% Plot the objective function ezplot(objFun, [-3,3]);

% Search for a minimum between -3 and 0
[x, val] = fminbnd(objFun, -3, 0)

### Minimization. Example 1-D

```
\% Search for a minimum between -3 and 0
>> [x, val] = fminbnd(objFun, -3, 0)
x =
-2.3562
val =
-1.4142
% Find for a maximun between -1 and 2
>> [x, val] = fminbnd(@(x) - objFun(x), -1, 2)
x =
0.7854
val =
```

-1.4142

#### Zero Finding. Example 2-D



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#### Minimization. Example 2-D

```
% Define the objective function as an anonymous
   function
objFun = Q(x) sin(x(1))*cos(x(2));
objFunPlot = Q(x,y) sin(x).*cos(y);
```

% Plot the objective function ezsurf(objFunPlot, [-3,3]);

```
% Search for a minimum with guess (0,0)
[x, val] = fminsearch(objFun, [0,0])
```

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#### Minimization. Example 2-D

```
% Search for a minimum with guess (0,0)
>> [x, val] = fminsearch(objFun, [0,0])
x =
-1.5708 0.0000
val =
-1.0000
% Search for a maximum with guess (0,0)
>> [x, val] = fminsearch(@(x) - objFun(x), [0,0])
x =
1.5708 - 0.0000
```

```
val =
```

```
-1.0000
```

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# Configuring the Optimizer

- The optimizer functions can be configured by passing them an *options* structure.
- The most important ones are:
  - Display: to display output at each iteration, only the final output, or only if there is a problem.
  - Tolerance both of the X and the Function Value.
  - Maximum number of iterations.
  - etc.
- Options structures are created with the **optimset** command.
- The full list of options is available at: http://www.mathworks.com/help/matlab/ref/optimset.html or typing doc optimset

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### Configuring the Optimizer. Example

```
% Define the objective function as an anonymous
function
objFun = @(x) sin(x(1))*cos(x(2));
```

```
% Configrue the optimizer
% Display results at each iteration
options = optimset('Display','iter');
```

```
% Search for a minimum with guess (0,0)
[x, val] = fminsearch(objFun, [0,0], options)
```

### Configuring the Optimizer. Display Options

#### options = optimset('Display', value)

Value	Displays
'off'	Nothing
'notify'	A message only if the function fails
'final'	Only the final message
'iter'	Output at each iteration

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#### Steps in optimization

- Look at your problem: It is a zero finding problem or a minimization one? Does the problem have constraints?
- 2 Choose the adequate optimizer for the problem you have.
- Onfigure the optimizer.
- Oefine an initial guess for the solution.
- Optimize it!.
- O Check if results are correct or if they look strange.

#### References

#### References



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